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Spatial ecological complexity measures in GRASS GIS

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Abstract

Good estimates of ecosystem complexity are essential for a number
of ecological tasks: from biodiversity estimation, to forest structure
variable retrieval, to feature extraction by edge detection and genera-
tion of multifractal surface as neutral models for e.g. feature change
assessment. Hence, measuring ecological complexity over space be-
comes crucial in macroecology and geography. Many geospatial tools
have been advocated in spatial ecology to estimate ecosystem com-
plexity and its changes over space and time. Among these tools, free
and open source options especially offer opportunities to guarantee
the robustness of algorithms and reproducibility. In this paper we will
summarize the most straightforward measures of spatial complexity

36 available in the Free and Open Source Software GRASS GIS, relating
37 them to key ecological patterns and processes.

38 **keywords:** Free and Open Source Software; remote sensing; spatial
39 complexity; spatial ecology.

40 1 Introduction

41 In spatial ecology, the complexity of ecosystems, and the changes in that
42 complexity over time, are critical issues. Mapping and modelling landscape
43 heterogeneity over space and time has been acknowledged as one of the most
44 powerful methods to gather information about underlying changes in abiotic
45 and biotic components of ecosystems including land cover, land use, vegeta-
46 tion and soil.

47 Experimental manipulations to effectively measure complexity in the field
48 are difficult from both a cost and a logistical point of view, and, depending
49 on the scale of the studied ecological problem, may become impossible (Roc-
50 chini et al., 2013a). Therefore, proxies for ecological complexity are needed.
51 Reliable proxy variables which are available at large scale can allow upscaling
52 of complexity estimates and a clearer focus on processes that act at multiple
53 spatial and temporal scales (Sagarin and Pauchard, 2009; Amici, 2011).

54 In view of these requirements, remote sensing represents a crucial source
55 of information for measuring ecological complexity for several reasons, in-
56 cluding: i) availability at multiple spatial scales (grain, pixel size) at the
57 same time, ii) high temporal resolution, iii) coverage of large areas within
58 relatively short timespans (Wegmann et al., 2014). As an example, remote
59 sensing data have long been used for ecological applications such as biodiver-
60 sity estimation, ecosystem management, restoration, hydrological modelling,
61 land use mapping and climate change detection (e.g. Skidmore et al. (2015)).

62 Land and water resources managers around the world can now observe
63 shifts in landscapes, nightscapes and waterscapes (Venot et al., 2007; Molle
64 et al., 2012; Marcantonio et al., 2015) by combining remote sensing with
65 spatio-temporal modeling (McCartney and Arranz, 2007; Ali et al., 2014).
66 It is particularly important to monitor those resource constraints which can
67 generate pressure on ecosystem services from various anthropogenic actors
68 (Molle et al., 2012). Many software packages attempt to evaluate patterns of
69 land use change and its impacts on land- and waterscapes (Baker et al., 1991;
70 Rubin et al., 2003), and some of these packages consider long term dynamics
71 (Coulthard, 2001).

72 A review of the field shows some independent specialized software and
73 some integrated software, such as OSSIM, Orfeo ToolBox, Opticks, and

74 GRASS GIS. There is a growing demand from the scientific community as
75 well as public and funding bodies for full reproducibility in research, and
76 producing the exact set of code and data used in a research goes a long way
77 towards permitting both peer-review and future research (Chemin et al.,
78 2015). Reproducibility and robustness of software algorithms are two funda-
79 mental requirements to allow the continuity of scientific methods over time
80 (Petras et al., 2015).

81 In this paper we will summarize the most straightforward measures of
82 spatial complexity available in the Free and Open Source Software GRASS
83 GIS, and relate them to the potential estimation of key ecological patterns
84 and processes.

85 **2 GRASS GIS based algorithms for complexity** 86 **measurement from remote sensing**

87 **2.1 Why GRASS GIS?**

88 GRASS GIS (Geographical Resources Analysis Support System, Neteler et al.
89 (2012)) was first developed by the U.S. Army Construction Engineering Re-
90 search Laboratories in the eighties. It allows managing and analyzing geo-
91 graphical data by 500 dedicated modules.

92 Worldwide contributions from the scientific community based on a free
93 open source software (FOSS) license, available from 1999, and on an online
94 source code repository (Concurrent Versioning System at that time) ren-
95 ders GRASS GIS one of the most cutting-edge projects of the Open Source
96 Geospatial Foundation (OSGeo, founded in 2006).

97 In this research we will describe and illustrate the most powerful modules
98 in GRASS GIS to measure spatial complexity from an ecological perspective.
99 The methods are applicable to any raster imagery, but in ecology the datasets
100 which are most commonly processed in these contexts are digital elevation
101 models, categorical land-use maps or continuously-valued imagery derived
102 from remote sensing, representing variables such as vegetation density.

103 We will make use of the free dataset called “North Carolina” available
104 online at
105 <http://grass.osgeo.org/download/sample-data/> together with additional Land-
106 sat ETM+ data, using GRASS GIS version 7.0.

107

108 2.2 Geometrical complexity: detecting edges

109 Geometrical complexity is a landscape property which is used as one of
 110 the main heuristics to distinguish individual patches by objective methods.
 111 Patches may be identified by detecting edges at different spatial scales under
 112 a hierarchical criterion (Burnett and Blaschke, 2003).

113 Current Object Based Image Analysis (OBIA) techniques generally build
 114 on edge detection (Thomas, 2010). In this section we will illustrate the most
 115 powerful techniques available in GRASS GIS to detect edges relying on: i)
 116 zero-crossing edge detection, ii) building vector contours from raster maps,
 117 iii) edge density and contrast weighted edge density calculation, iv) Canny
 118 filtering, v) Hough transforms.

119 2.2.1 Zero-crossing "edge detection" raster function for image 120 processing: the `i.zc` function

121 The `i.zc` function allows users to locate boundaries using the zero-crossing
 122 algorithm based on the following arguments:

123

```
i.zc input=string output=string [width=integer]
    [threshold=float] [orientations=integer]
```

124

125 where an `input` raster is converted to a zero-crossing raster map (`output`)
 126 with a specified Gaussian filter dimension (default is 9, but it can be changed
 127 by the argument `width`) and sensitivity (default is 10, but it can be changed
 128 by the argument `threshold`, together with the optional specification of
 129 the number of azimuth directions to be categorized (optional parameter
 130 `orientations`, default equals 1). Notice that, according to GRASS nota-
 131 tion, arguments in square brackets are optional.

132 The procedure to find the edges in the image is based on the calculation of
 133 the Fourier transform of the image (see e.g. Rocchini et al. (2013b)) and the
 134 application of a Laplacian filter. The image is further processed, searching
 135 for local changes from positive to negative values. Where the change value
 136 crosses zero with respect to a defined threshold the pixel is marked as an
 137 edge.

138 As an example, using a Landsat7 ETM+ band as input, the output crossing
 139 edges are derived using the command shown below:

140

```
i.zc lsat7_2002_40 output=lsat7_2002_40_zerocrossing
```

141

142 leading to the output shown in Figure 1.

143 **2.2.2 Producing a vector map of specified contours from a raster** 144 **map by `r.contour`**

145 In some cases, edge detection relates to linear objects in the imagery that
146 are defined by a series of points having similar properties, e.g. the same
147 elevation. As an example, generating contours from an input raster map is
148 done using the `r.contour` function as shown below:

149

```
r.contour input=string output=string step=float
minlevel=float
maxlevel=float [levels=float[,float,...]] [cut=integer]
```

150

151 where `input` and `output` are the original raster map and the output vector
152 contours map respectively, `step` is the relative increment between adjacent
153 contours values, `minlevel` and `maxlevel` are the minimum and maximum
154 values in the image. These values can be derived using the function `r.info`.

155 As an example, let `elevation` be the input raster map; its contours might
156 be derived simply as:

157

```
r.contour input=elevation output=elev_contours minlevel=50
maxlevel=160 step=10
```

158

159 producing the map shown in Figure 2.

160 **2.2.3 Calculating edge density index on a raster map: `r.li.edgedensity`**

161 Given a raster map, `r.li.edgedensity` is able to calculate a perimeter-to-area
162 ratio, creating polygons based on a 4-neighbour rule. In the ecological con-
163 text, such an approach is often applied to maps of land use in order to
164 estimate the heterogeneity of the landscape and the fragmentation of its
165 components.

166 The formula used is simply:

167

$$E = \frac{\sum(e_k)}{A} \times 10000 \quad (1)$$

168

169 where k =patch type and e_k =total edge length related to class k , A =total
170 landscape area.

171 As in all the `r.li` functions in GRASS GIS, a configuration file (argument

172 `conf`) specifying the grain and the extent of analysis should be provided. This
 173 can be generated using the command `g.gui.rlisetup` which allows the user
 174 to choose the grain and extent of the calculation. In this paper we will rely
 175 on local moving windows *sensu* Hagen-Zanker (2016).

176 The final command is as follows:

177

```
r.li.edgedensity map=name conf=name output=name
```

178

179 **2.2.4 Calculating contrast weighted edge density index on a raster** 180 **map: `r.li.cwed`**

181 By contrast with simple edge density, contrast weighting allows a weighting
 182 of the calculation based on:

183

184

$$CWED = \frac{\sum e_{ik} \times d_{ik}}{Area} \times 10000 \quad (2)$$

185

186 where k =attribute under consideration, e_{ik} =edge density between patch types
 187 i and k , d_{ik} =dissimilarity between patch types i and k , and Area=total land-
 188 scape area.

189 In the ecological context, this varying dissimilarity is important because it
 190 allows certain types of boundary to be given more importance: for example,
 191 a boundary between hard surface and grassland represents more of a barrier
 192 to some dispersing species than a boundary between wet and dry grassland.

193 **2.2.5 Canny edge detector**

194 The `i.edge` function uses the edge detector defined by Canny (1986) to detect
 195 edges in a raster map. The Canny edge detector is considered optimal by
 196 Sonka et al. (1999) based on the following criteria: i) important edges cannot
 197 be omitted and only actual edges can be detected as edges, ii) the difference
 198 in position of the actual and the detected edge is minimal, iii) there is only
 199 one detected edge for an actual edge in the original image. The Canny edge
 200 detector first reduces the noise in the raster map using a Gaussian filter. Then
 201 it computes gradient defined by an angle and magnitude. The next step is
 202 non-maximum suppression, which preserves only those pixels with magnitude
 203 higher than magnitude of other pixels in the direction of the gradient. The
 204 final step extracts significant edges by thresholding with hysteresis. The
 205 Canny edge detector can be applied using the following command:

```
i.edge input=name output=name [angles_map=name]
[low_threshold=float] [high_threshold=float] [sigma=float]
```

206

207 where `input` is an image, `output` is a raster map containing the de-
 208 tected edges, `angles_map` is a raster map containing the angle of the image,
 209 `sigma` is the size of the moving window (kernel) used and `low_threshold`
 210 and `high_threshold` are used during the thresholding with hysteresis as fol-
 211 lows: values over the `high_threshold` are kept; values under `low_threshold`
 212 are removed; values in between these constants are kept only when the pixel
 213 touches another pixel with value above `high_threshold`.

214 The result of `i.edge` function is a binary raster image where edges are
 215 represented as rasterised lines exactly one pixel wide. The detected edges
 216 can be used for further analysis using for example, the `r.neighbors` func-
 217 tion which can extract areas with high or low edge density. In Figure 3, areas
 218 with many edges are associated with developed areas, while areas with low
 219 density indicate natural areas. The result can be used also as an input for a
 220 Hough transform.

221 2.2.6 Hough transform

222 The Hough transform is a feature extraction technique which identifies straight
 223 line segments from a raster image and outputs them as vector features. Such
 224 a technique is applicable to edges detected and rasterised using the methods
 225 described above (Hough, 1962; Duda and Hart, 1972). Points in the real
 226 space which are assumed to represent points on an edge are transformed into
 227 a Hough plane applying the following equation to describe a line:

228

$$x \cos \theta + y \sin \theta = r \quad (3)$$

229 where r is the length of a normal from the origin in the Hough plane to the
 230 line and θ is the angle of the normal.

231 Points in the original image which belong to one line result in sinusoidal
 232 curves intersecting in one point in the transformed image as in Figure 4. The
 233 coordinates of this point describe the parameters r and θ of the line, and its
 234 value represents the number of points on the line.

235 The `r.houghtransform` function in GRASS GIS uses the 'identify and
 236 remove' method proposed by Fiala (2003) which identifies the most promi-
 237 nent lines in a raster image and outputs the coordinates of the associated line
 238 segments. Galambos et al. (2000) showed that the detection is significantly
 239 faster when the gradient direction of the edge is provided as well. GRASS
 240 GIS uses this extension when the direction is available.

241 Using the Hough transform, GRASS GIS detects the linear features using
242 the following:

243

```
r.houghtransform input=name output=name [angles=name]  
[hough_image=name] [max_gap_count=integer]  
[min_segment_length=integer]
```

244

245 where **input** is a raster map containing edges, **output** is a vector map
246 containing detected straight line segments, **angles** is an optional input for
247 speedup, **hough_image** is an optional output for visual inspection of the
248 Hough transform, **max_gap_count** is a maximal allowed number of gaps in
249 one line segment and **min_segment_length** is a minimal allowed length of
250 one line segment. There are several other parameters which ensure fine control
251 over the number and properties of the detected lines.

252 The typical input to a Hough transform is a raster image containing
253 thin edges detected e.g. by the **i.edge** function. The straight (and, depending
254 on configuration, more or less long) lines which result from the
255 **r.houghtransform** function can be used as indicators of man-made features
256 such as the straight parts of a highway visible in Figure 5. The
257 **r.houghtransform** can be also applied to terrain or surface contours to retrieve
258 straight lines in terrain, possibly associated with roads, buildings and
259 other man-made structures. Furthermore, Hough transform can be used to
260 automatically detect geological lineaments (Vasuki et al., 2014; Wang and
261 Howarth, 1990).

262 2.3 Local diversity in a neighbourhood

263 Calculating local diversity is important to detect spots of diversity at a local
264 scale. As an example, in biodiversity research, this is known as α -diversity
265 and it is a widely-used metric in ecology (Rocchini et al., 2010).

266 2.3.1 Local statistics by **r.neighbors**

267 The **r.neighbors** command provides the means to compute a variety of local
268 statistic, including: average, median, mode, minimum, maximum, range,
269 standard deviation, sum, count, variance, diversity (i.e. the number of different
270 values in the neighbourhood with respect to the central pixel), interspersion
271 (weighted diversity), first quartile, third quartile, user-specified
272 quantiles.

273 In the case where one is interested in a measure of complexity over space,

274 standard deviation in a neighbourhood might be simply calculated as follows:

275

```
r.neighbors input=name output=name method=sttdev
[size=value]
```

276

277 The size may be changed to enlarge the window of analysis, starting with
278 a default of 3×3 cells.

279

280 **2.3.2 Information-theory based statistics: `r.li.shannon`, `r.li.pielou`,**
281 **`r.li.simpson`, `r.li.renyi`**

282 GRASS GIS is capable of handling common Information-theory based statis-
283 tics such as Boltzman or Shannon-Weaver entropy H (Shannon, 1948), Pielou
284 evenness (Pielou, 1966) and Simpson's reversed dominance (1-D, Simpson
285 (1949)).

286 Different diversity measures are generally used to summarise large multi-
287 variate data sets, providing for one potentially meaningful single value. Such
288 an approach inevitably results in information loss, since no single summary
289 statistic can characterize in an unequivocal manner all aspects of diversity
290 (Ricotta, 2005; Marcantonio et al., 2014). Rocchini and Neteler (2012) ad-
291 dressed such problems when measuring diversity from a satellite image relying
292 on the richness and relative abundance of Digital Numbers (DNs), by only
293 using entropy-based metrics. In particular, they observed: i) the intrinsic
294 impossibility of discriminating among different ecological situations with one
295 single diversity index, and ii) the impossibility of understanding whether di-
296 versity of different sites is more related to differences in richness or in relative
297 abundance of DN values. As an example, they provided a theoretical case in
298 which the same value of the Shannon index would actually be related to very
299 different situations in terms of DN's richness and abundances (see Figure 2 in
300 Rocchini and Neteler (2012)). In general, to solve this issue, combining these
301 entropy-based indices with evenness-based metrics might lead to an increase
302 in their information content. In this regard, the most commonly-used metric
303 is the Pielou evenness index $J = \frac{-\sum p \times \ln(p)}{\ln(N)}$ (Pielou, 1969), which can be
304 rewritten as: $J = \frac{H}{H_{max}}$ since it contains the maximum possible diversity
305 ($\ln(N)$), for N DN's.

306 All the previously described metrics based on Information theory only
307 supply point descriptions of diversity. By contrast, Rényi (1970) firstly in-
308 troduced a generalized entropy metric, $H_\alpha = \frac{1}{1-\alpha} \times \ln \sum p^\alpha$ which shows a
309 high flexibility and power because a number of popular diversity indices are

310 special cases of H_α . In mathematical terms, if we consider e.g the variation
 311 of α from 0 to 2:

$$H_\alpha = \begin{cases} \alpha = 0, H_0 = \ln(N) \\ \alpha = 1, H_1 = -\sum(p \times \ln(p)) \\ \alpha = 2, H_2 = \ln(1/D) \end{cases} \quad (4)$$

312 where N = number of Digital Numbers (DNs), p = relative abundance of
 313 each DN value, D = Simpson index.

314 Concerning the results attained when $\alpha=1$, the Shannon index is de-
 315 rived according to the L'Hôpital's rule of calculus (see Ricotta (2005). Rényi
 316 generalized entropy represents a continuum of diversity measures Ricotta and
 317 Avena (2003)), meaning that it is possible to maintain sensitivity to both rare
 318 and abundant DN's, and it is more responsive to the commonest DN's while
 319 α increases. Varying α can be viewed as a scaling operation, not in a real
 320 space but in the data space.

321 As far as we know, GRASS GIS is the only software capable of calculating
 322 generalized measures of diversity such as the Rényi formula in a 2-dimensional
 323 space, based on the following function:

324

```
r.li.renyi conf=conf3 in=landsat.pc1 out=landsatrenyi
alpha=2
```

325

326 Changing the parameter α will change the behaviour of the formula, gen-
 327 erating different maps of diversity as represented in Figure 6, representing
 328 a continuum of diversity values over space instead of single measures. In-
 329 creasing alpha values in the Rényi diversity index will weight differences in
 330 relative abundance more heavily than differences in simple richness.

331 2.4 Texture-based metrics (*sensu* Haralick et al. (1973))

332 2.4.1 Generating images with textural features from a raster map:

333

```
r.texture
```

334 GRASS GIS permits computation of all the local textural features that may
 335 be calculated in a neighborhood of pixels, described in the benchmark paper
 336 by Haralick et al. (1973): i) the angular second moment, as a measure of local
 337 homogeneity; ii) the contrast, a gray-level variation with respect to neighbor
 338 pixels; iii) the correlation, a linear dependency value; iv) the variance in
 339 the neighboring moving window (see also `r.neighbors`); v) the entropy, an
 340 index of randomness; vi) the sum average; vii) the sum entropy; viii) the sum

341 variance; ix) the difference in variance; x) the difference in entropy; xi) the
 342 inverse distance moment, i.e. the inverse of the previously described contrast
 343 measure; xii) the maximal correlation coefficient. We refer to Haralick et al.
 344 (1973) for a detailed description of all the measures.

345 The approach to be used can be declared as the `method` parameter of the
 346 function `r.texture`, as follows:

347

```
r.texture input=landsat.pc1 method=asm,contrast,corr,var,idm,
sa,se,sv,entr,dv,de,moc1,moc2 output=texture
```

348

349 Figure 7 presents all the aforementioned maps generated from a Landsat
 350 ETM+ image.

351 Further, the following R code can show the amount of correlation among
 352 different measures once data are imported in R by the `rgrass7` package, as
 353 shown below:

354

```
# require the rgrass7 library to import GRASS data in R
require(rgrass7)
# import data textureset <- readRAST(c("texture_ASM",
"texture_Contr","texture_Corr",
"texture_Var",
"texture_Entr","texture_SA","texture_SE","texture_SV",
"texture_DV", "texture_DE", "texture_IDM",
"texture_MOC-1"), cat=c(F,F,F,F,F,F,F,F,F,F,F,F))
# require the hexbin package to do an hexagon binning between
variables
hbin <- hexbin(textureset$texture_IDM,
textureset$texture_Contr, xbins=50)
plot(hbin)
```

355

356 Figure 8 shows the correlation trends found applying this code, while
 357 the hexagon binning plots are shown in the Supplementary Material of this
 358 manuscript. The majority of the variables were strongly correlated (Figure 9,
 359 generated by the `corrplot` package in R), showing the high multicollinearity
 360 of the texture measures system. Once such relations are used to plot maps
 361 derived from each other, the similarity is apparent. Figure 10 shows the
 362 map of estimated Sum Entropy from Entropy (by applying a linear model,
 363 $R^2=0.9023$, $p<0.001$) which is similar to the original one, while residuals
 364 distribution follows, as expected, the magnitude of the values of the predicted

365 variable. Hence, when modelling ecosystem complexity, texture measures
 366 should be used with care since, by their very nature, they are expected to be
 367 correlated with each other.

368 2.5 Detecting heterogeneity in synthetic spaces

369 2.5.1 Fast Fourier Transforms (FFT) for image processing: `i.fft`

370 The use of transforms in frequency spaces to measure variation in a signal has
 371 long been acknowledged. While methods exist based on orthonormal series
 372 (e.g. rectangular decomposition of waves, Walsh (1923)), the most commonly-
 373 used methods rely on continuous waves, mainly based on the Fourier trans-
 374 forms (Fourier, 1822).

375 When seeking a method to detect landscape change based on continuous
 376 instead of classified information, one should rely on a (continuous) function
 377 which does not require a) a-priori field information nor ii) a specific model
 378 based on the data being used. In view of this, Fourier transforms (Fourier,
 379 1822) may represent the best algorithmic solution.

380 Let $f(x)$ be a continuous function described into a spatial domain. Based
 381 on the Fourier theorem (Fourier, 1822) every $f(x)$ can be transformed into a
 382 continuum of sinusoidal functions of varying frequency, as follows:

$$F(\omega) = \int_{-\infty}^{\infty} f(x)e^{-2\pi i\omega x} dx \quad (5)$$

383 where ω = frequency, also known as radian frequency since it is expressed
 384 in radians per spatial units. In mathematical notation for discrete Fourier
 385 transforms $f(x)F(\omega)$. Extending Eq. (4) to two dimensions implies consid-
 386 ering a two-dimensional function $f(x,y)$, e.g. a raster matrix. Its Fourier
 387 transform turns out to be:

$$F(\omega, \nu) = \int \int_{-\infty}^{\infty} f(x, y)e^{-2\pi i(\omega x + \nu y)} dx, dy \quad (6)$$

388 where ω, ν = frequency coordinates.

389 Considering as an example a single raster image (e.g. the first Principal
 390 Component of a Landsat scene) the command to be used to calculate its
 391 Fourier transform is straightforward:

392

```
i.fft input_image=lsat_pca1 real=lsat_pca1_real  
imaginary=lsat_pca1_imag
```

393

394 where `real`=real part of Eq.(4) and Eq.(5) and `imaginary`=imaginary
 395 part of Eq.(4) and Eq.(5), both stored as raster maps. An example of the
 396 output is provided in Figure 11.

397 In the Fourier space, high frequency values (high heterogeneity) are at the
 398 border of the image while low frequency values (high homogeneity) are at
 399 the center. Hence the higher the value of pixels at the border, the higher the
 400 heterogeneity / complexity of the whole image.

401 2.6 Testing complexity against random surfaces

402 Observed ecological patterns can be tested against random patterns by calcu-
 403 lating the deviation from random expectations in two dimensions (Hanspach
 404 et al., 2011). To accomplish this goal, different kinds of lattice surfaces can
 405 be generated, including: completely random surfaces, gaussian distributed
 406 and fractal surfaces with a predefined fractal dimension.

407 2.6.1 Generating random surfaces by `r.random.surface`

408 Random surfaces can be generated by the following basic function and argu-
 409 ments command:

410

```
r.random.surface output=string [distance=value]
[exponent=value]
```

411

412 where `distance` represents the maximum distance of spatial correlation
 413 among pixels and `exponent` represents the exponential decay of values over
 414 space. As an example, Figure 12 represents a random surface generated by
 415 the aforementioned command. As an example, a Landsat image might be
 416 tested against this to find areas where similar values are especially clumped
 417 and significantly deviate from random expectations over space.

418 2.6.2 Generating gaussian random number maps by `r.surf.gauss`

419 A more sophisticated but still straightforward neutral model is represented by
 420 a surface whose values have a normal distribution in two dimensions.

421 This can be created by the following command:

422

```
r.surf.gauss output=name [mean=value] [sigma=value]
```

423

424 where the mean and the standard deviation (σ) can be defined a-priori
425 (Figure 12).

426 **2.6.3 Neutral landscapes by fractal surfaces of a given fractal di-** 427 **mension: `r.surf.fractal`**

428 Following Mandelbrot (2006), surfaces with a given fractal dimension from 2
429 to 3 might represent severe differences in their roughness / complexity (Imre
430 et al., 2011). Such surfaces can be generated in GRASS GIS by the function
431 `r.surf.fractal` by explicitly stating the fractal dimension according to the
432 parameter `dimension`, as:

```
433 r.surf.fractal output=name [dimension=value]  
[number=value]
```

434 A very useful parameter is represented by `number` which indicates the
435 number of intermediate surfaces one might want to generate to finally gather
436 a complete set of images of variable fractal dimension (Figure 12).

437 **3 Summary of the presented algorithms**

438 As described in this paper, there are many ways of defining complexity
439 (Anand and Tucker, 2003), and then measuring it. Every single measure of
440 complexity has a potential spatio-ecological application, in particular when
441 it is applied to remotely sensed imagery: from feature extraction by edge de-
442 tection (Zhang et al., 2005), to biodiversity estimation by information theory
443 (e.g. Rocchini et al. (2010)), to forest structure variable retrieval by textu-
444 ral analysis (Kayitakire et al., 2006), and multifractal surfaces generated as
445 neutral models for e.g. feature change assessment (Cheng, 1999).

446 We structured our paper to consider all the different aspects of complexity
447 in a variety of potential spatial fields of research: from geometrical complex-
448 ity to information theory-based measures, to texture, reprojected spaces and
449 random surfaces. In this paper we have accounted only for spatial complex-
450 ity, while ecological dynamics (temporal complexity) might be further stud-
451 ied using throughput analytic approaches based on e.g. i) stationary Markov
452 models (Tucker and Anand, 2005), ii) Monte Carlo analysis of multitemporal
453 series (Van Niel et al., 2005), or iii) Kohonen neural networks (Foody and
454 Cutler, 2006). The present paper mainly aims to describe features that are
455 already implemented in the GRASS GIS platform rather than describing the
456 procedure to implement new features. It can be stated that GRASS GIS
457 offers a concrete possibility of implementing new features rather easily using

458 its collection of excellent internal and external software libraries.

459 GRASS GIS offers the tools to compute a number of pre-existing mea-
460 sures of complexity, as well as the possibility to generate and evaluate new
461 ones, because of the free and open access to the source code. The mod-
462 ular software design of GRASS facilitates the introduction and sharing of
463 new functionalities without affecting the overall performance of the system.
464 Moreover, its scripting capabilities enable automated processing of a large
465 volume of data and wide-ranging use of the achieved results. In particular,
466 recent developments also allow GRASS users and developers to make use of
467 the Python programming language (Van Rossum (1995)) to introduce new
468 features.

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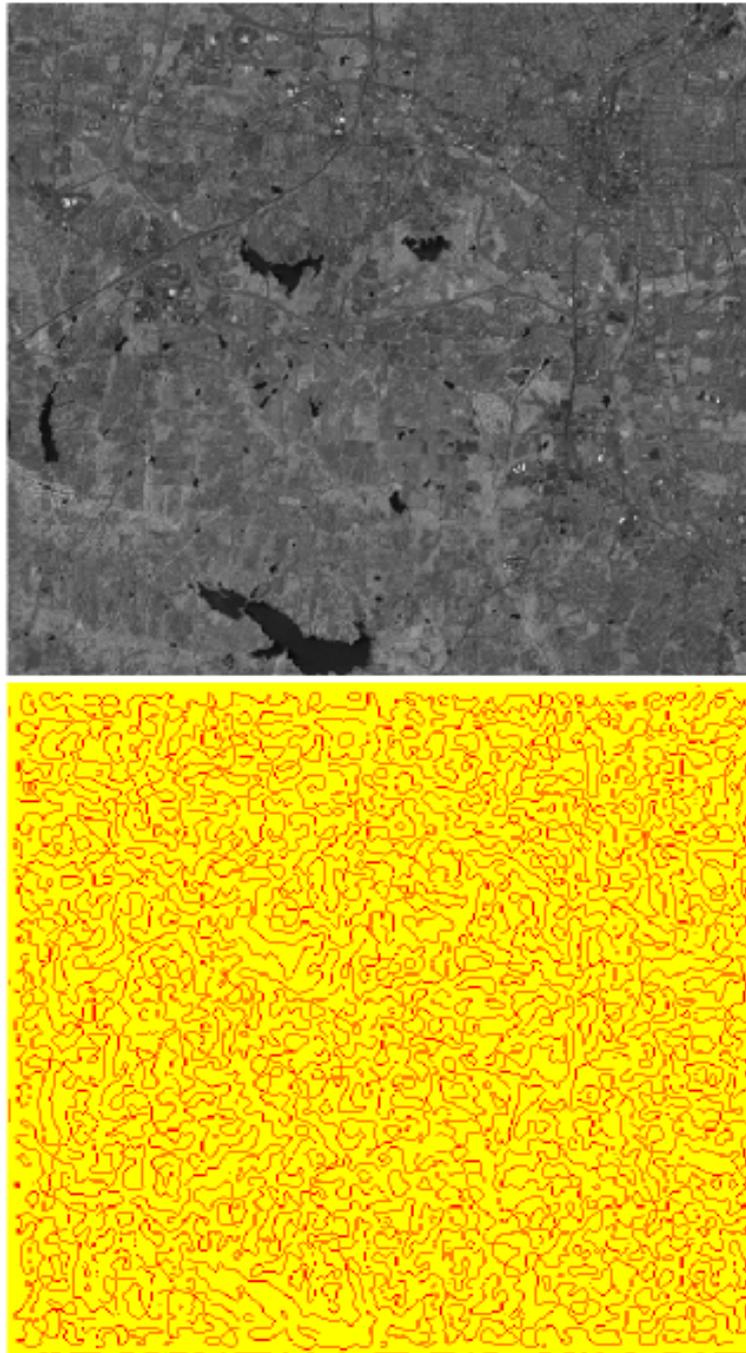


Figure 1: Zero-crossing “edge detection” raster function for image processing. A Landsat ETM+ band (near infrared) is processed and edges are revealed thanks to the `i.zc` function in GRASS GIS. Refer to the main text for additional information.

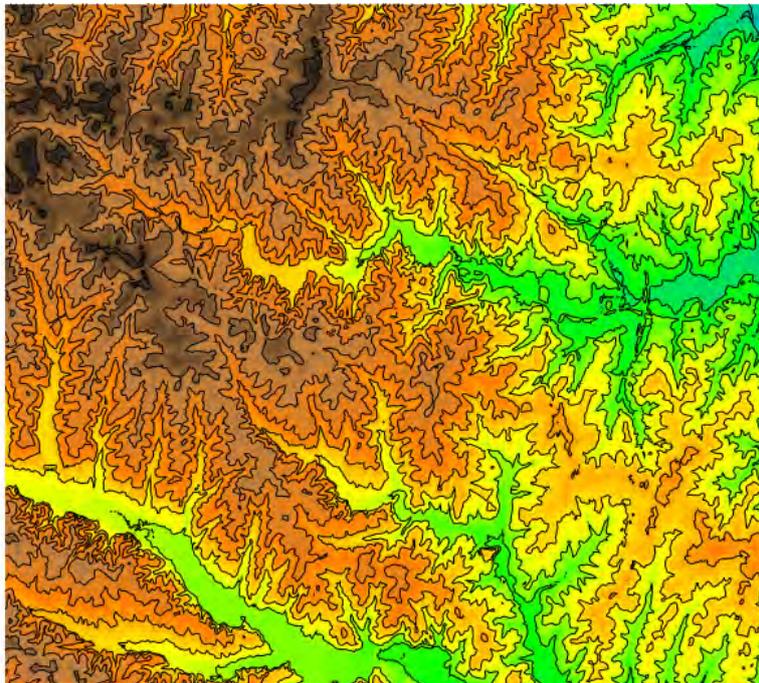


Figure 2: An elevation map from the GRASS North Carolina free dataset showing an elevation map and its contour with a step of 10 meters.

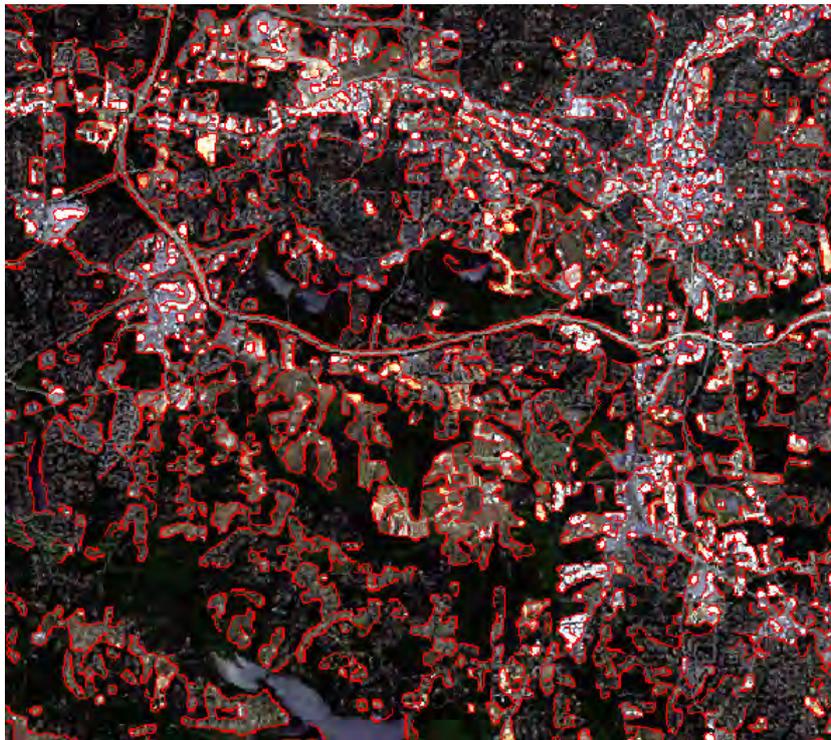


Figure 3: Edges (in red) detected by Canny edge detector on first component from PCA computed on 9 channels from Landsat 7, 2002, RGB channels in the background.

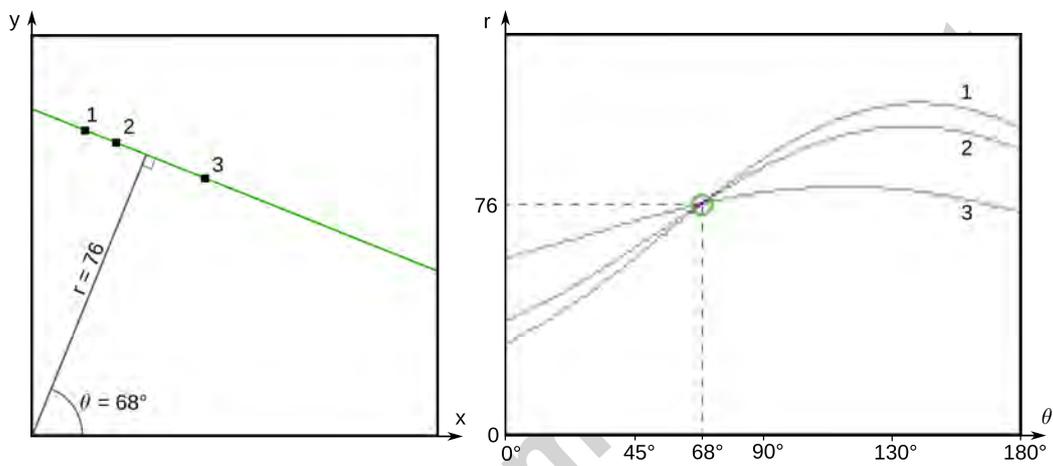


Figure 4: The linear feature to be automatically detected lies on the green line in the left image (coordinate space defined by $\{x,y\}$) and is represented only by several points (black pixels). Each point in the left image is transformed into a curve in the right image (coordinate space defined by $\{\theta,r\}$) by considering lines in all directions θ passing through the point. The coordinates of the intersection of the curves in the right image are the parameters of the line in the left image.

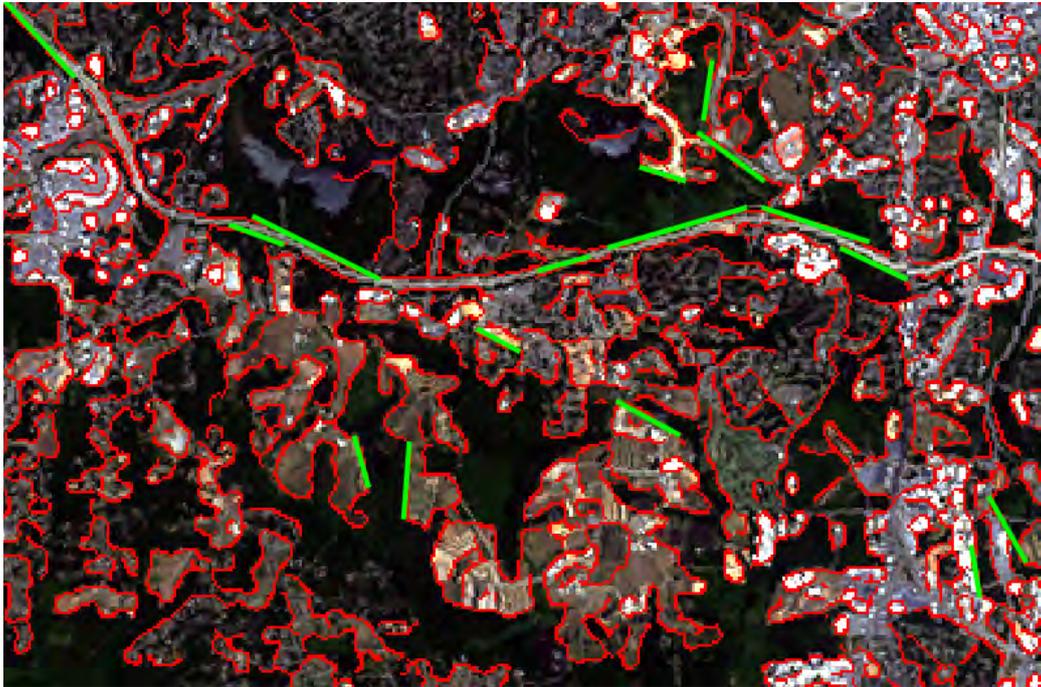


Figure 5: Detail of the central area from Figure 3 with lines obtained through Hough transformation (green) computed using the edges from Canny detector (red). Only the long lines, especially straight portions of the road, are detected.

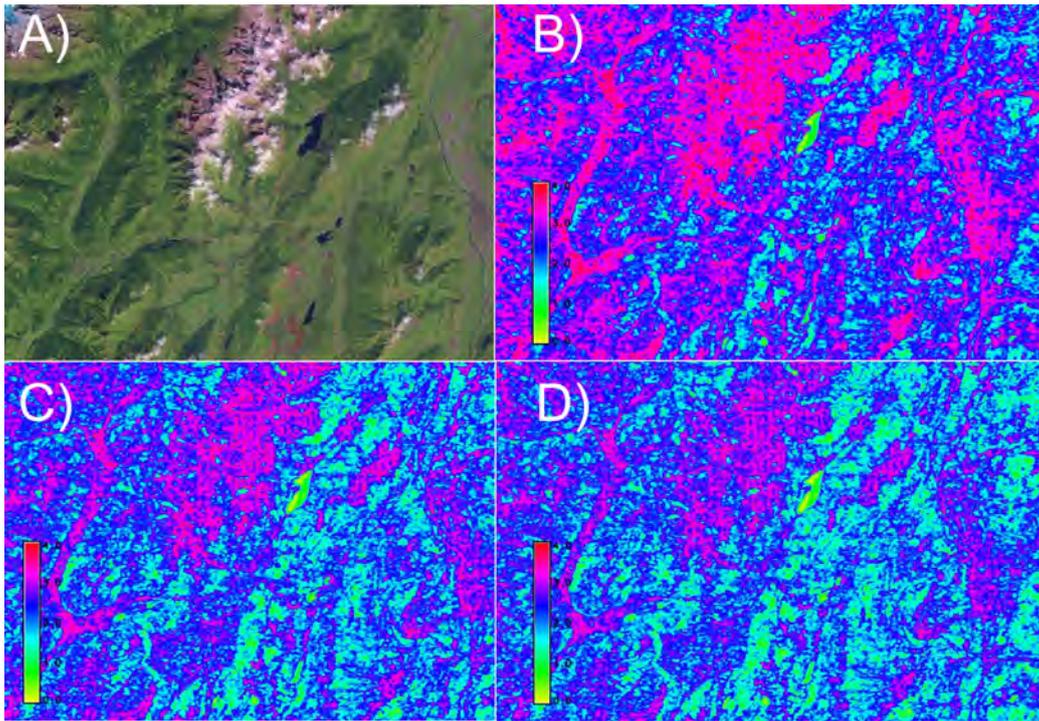


Figure 6: Rényi entropy can be calculated into GRASS 7.0 by the `r.li.renyi` command. In this example, starting from a Landsat ETM+ image, or a derivative like the first Principal Component, one might calculate different maps of Rényi entropy with different α values according to the formula $H_\alpha = \frac{1}{1-\alpha} \times \ln \sum p^\alpha$. In this case $\alpha=2$ (B), $\alpha=5$ (C), $\alpha=7$ (D). Refer to the main text for additional information.

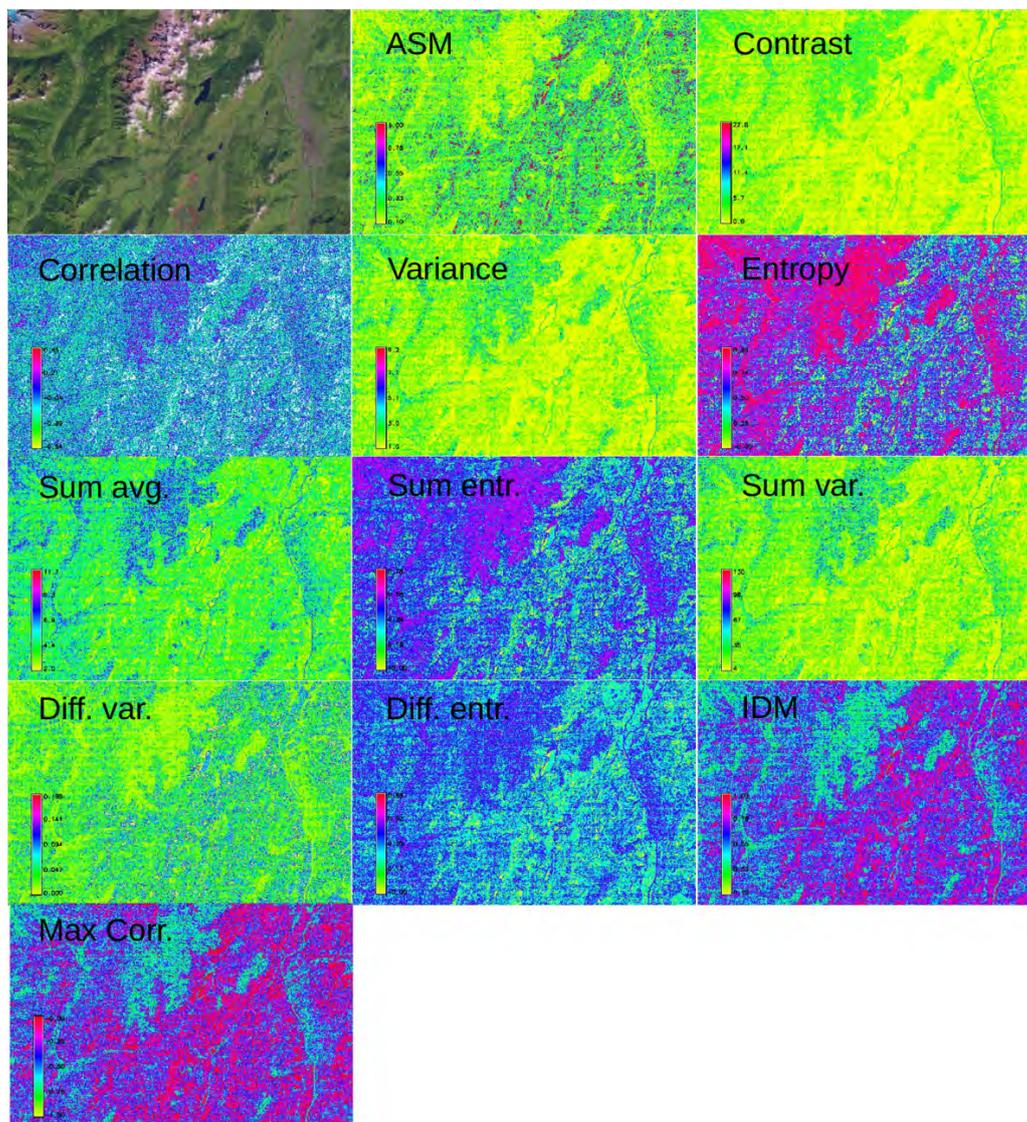


Figure 7: Different measures of texture as described in Haralick et al. (1973) starting from a Landsat ETM+ image of the Trentino region (Northern Italy). Acronyms: ASM = Angular Second Moment; IDM = Inverse Distance Moment

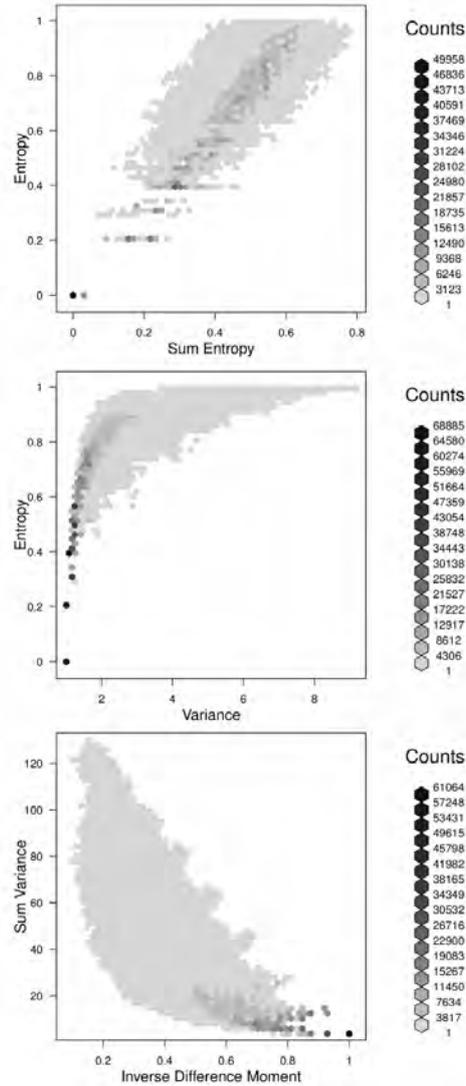


Figure 8: Hexagon binning showing the multicollinearity of a set of texture measures. Some of the main trends found, from top to bottom: linear relationship, power positive relationship, exponential decay. All the hexagon binning plots among the measured texture variables are available as Supplementary Material of this manuscript. If such variables are further used as predictors in e.g. a multiple regression model as complexity variables, they might be used with care since they basically carry the same (inverse, in this case) information.

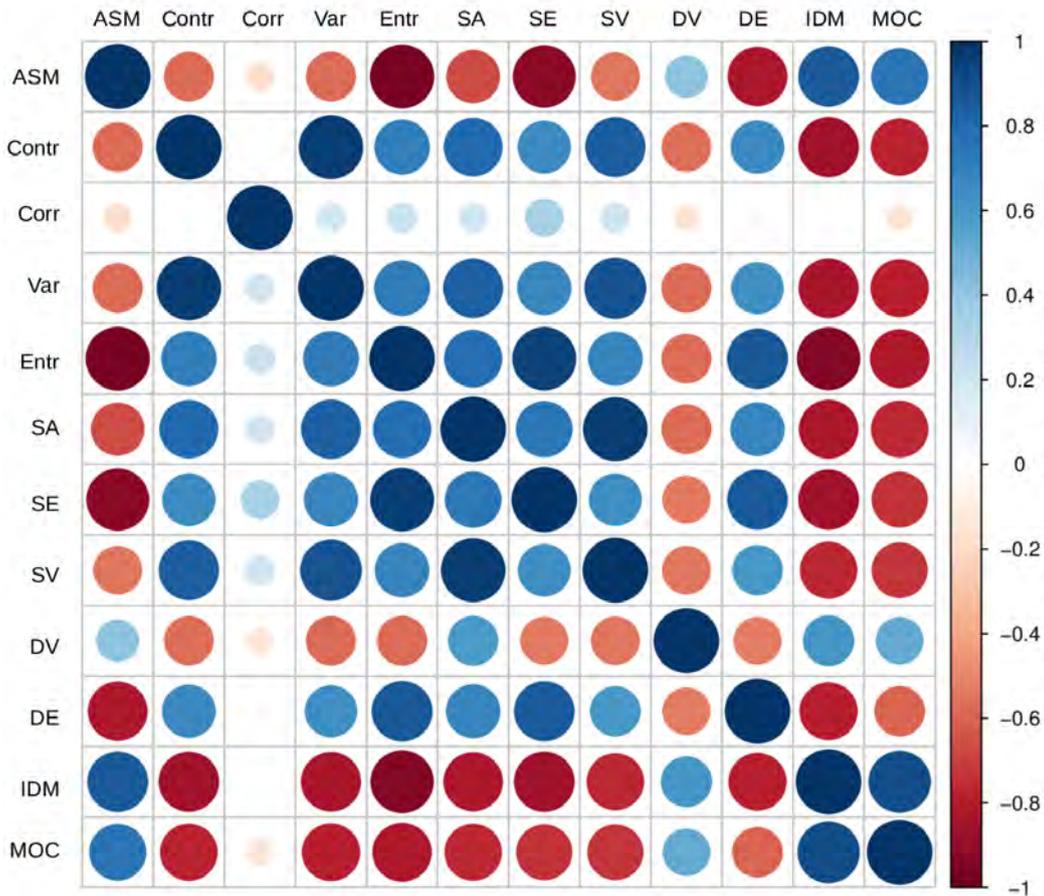


Figure 9: Correlations among the texture variables measured in GRASS GIS on a Landsat ETM+ of the Trentino region (Northern Italy), see Haralick et al. (1973), generated by the `corrplot` package in R. Only few variables showed a correlation near zero while most of them showed a high pairwise positive or negative correlation, demonstrating the basic multicollinearity of the texture measures system. ASM = Angular Second Moment, Contr = Contrast, Corr = Correlation, Var = Variance, Entr = Entropy, SA = Sum Average, SE = Sum Entropy, SV = Sum Variance, DV = Difference Variance, DE = Difference Entropy, IDM = Inverse Difference Moment, MOC = Information Measures of Correlation

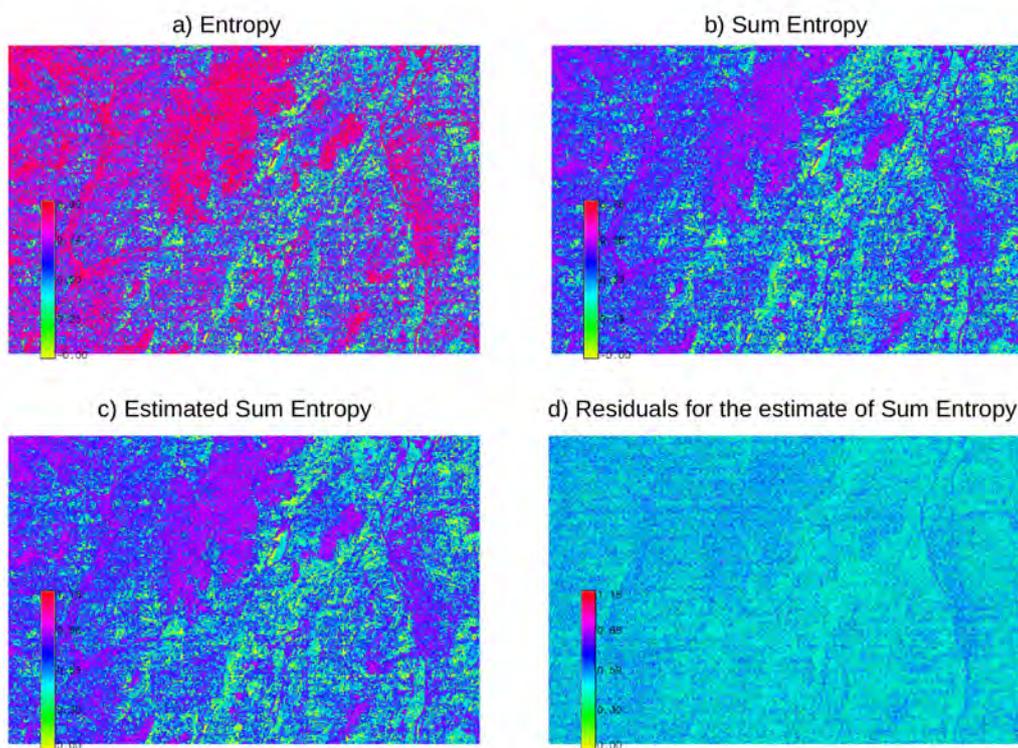


Figure 10: Example of the estimated values of a texture variable starting from another one. In this case, Sum Entropy is estimated from the Entropy variable, showing a similar pattern of the original Sum entropy image.

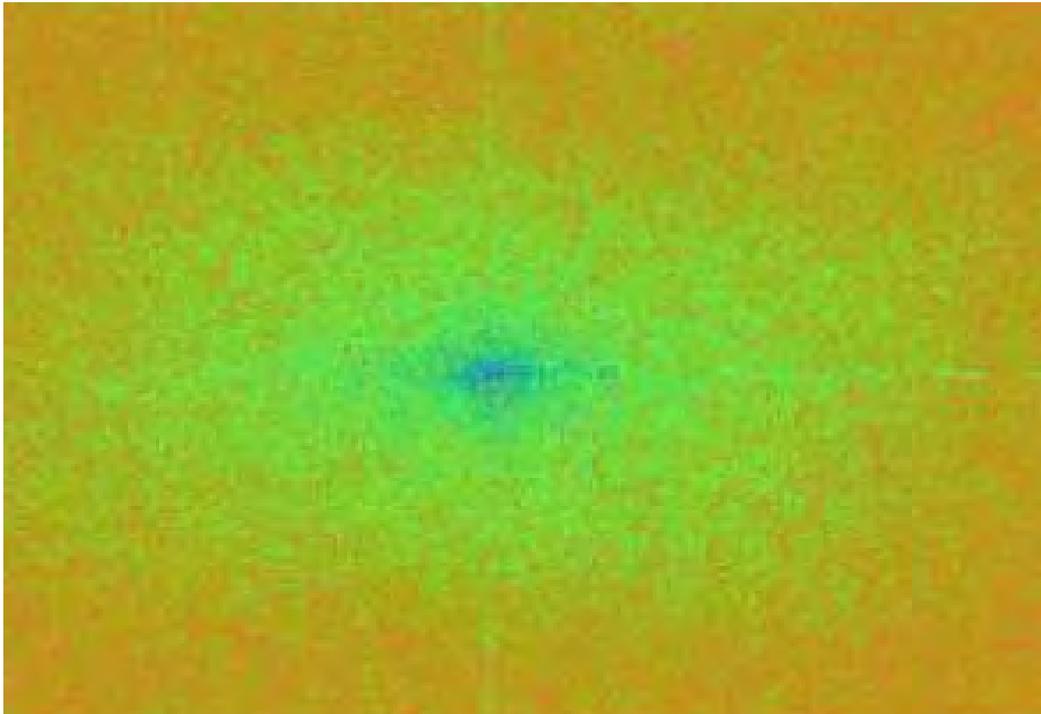


Figure 11: Fourier transform of a remotely sensed image. blue: high values. red: low values, green: medium values. The higher the green cloud the higher the magnitude of values toward the border of the image, i.e. the high frequency part. Hence the higher the green cloud the higher the heterogeneity of the image. (Please refer to the main text for additional information).

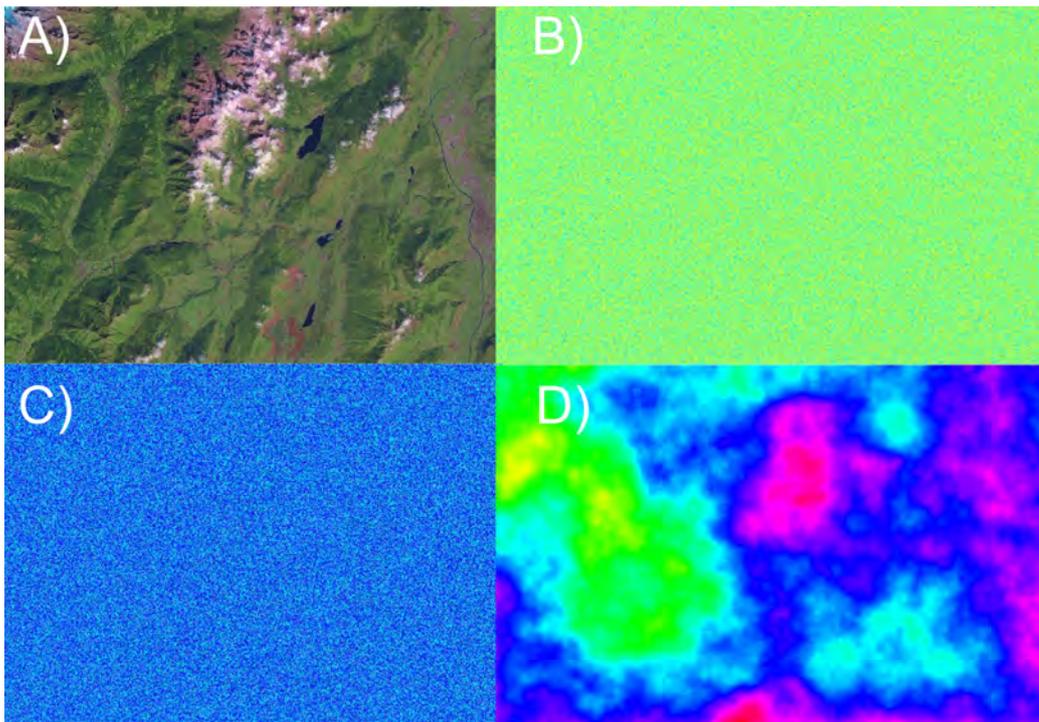


Figure 12: Random surfaces can be created as neutral models to test for patterns in real world images. As an example, patterns from a Landsat ETM+ of the Trentino region (Northern Italy) might be tested against a complete random surface (B), a gaussian surface (C), a fractal surface (D), fractal dimension 2.1.